

Mono-Higgs Detection of Dark Matter at the LHC

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Motivated by the recent discovery of the Higgs boson, we investigate the possibility that a missing energy plus Higgs final state is the dominant signal channel for dark matter at the LHC. We consider examples of higher-dimension operators where a Higgs and dark matter pair are produced through an off-shell Z or γ , finding potential sensitivity at the LHC to cutoff scales of around a few hundred GeV. We generalize this production mechanism to a simplified model by introducing a Z' as well as a second Higgs doublet, where the pseudoscalar couples to dark matter. Resonant production of the Z' which decays to a Higgs plus invisible particles gives rise to a potential mono-Higgs signal. This may be observable at the 14 TeV LHC at low $\tan\beta$ and when the Z' mass is roughly in the range 600 GeV to 1.3 TeV.

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I. INTRODUCTION

Dark matter (DM) contributes a large component of the mass-energy of the universe. The leading hypothesis is that most of the dark matter is in the form of stable, electrically neutral, massive particles, which interact at least gravitationally with baryons. If such a particle interacts non-gravitationally with standard model (SM) particles as well, for instance via the weak force, detecting it through high-energy collisions at particle accelerators is one of the most promising avenues towards identifying the specific nature of its detailed interactions. For instance, if DM production is kinematically accessible at the Large Hadron Collider (LHC), then missing energy signatures that deviate from SM predictions would provide compelling evidence of new stable, electrically neutral particles, and thus strong candidates for cosmological DM.

Various approaches to describing particle DM interactions have been explored in order to understand possible detection signatures at the LHC. The most detailed set of attempts include complete quantum field theories incorporating many new particles into the SM, for example supersymmetric dark matter [1]. Such top-down, or UV-complete, theories often have large sets of a priori undetermined additional parameters. Therefore, making confident phenomenological predictions can become very burdensome.

On the opposite end of the spectrum, one can assume that aside from the dark matter, any new heavy fields of the UV-complete theory can be integrated out and that the relevant physics can be described by an effective field theory (EFT). The effective field theorist thus proceeds by writing down a tower of non-renormalizable contact operators governing the DM interactions with SM particles. The underlying UV theory determines the coefficients of these operators, which in turn can be constrained in a model-independent way from experimental results and also be related in a simple way to relic density or direct detection predictions [2]. In addition to the

relative simplicity of constraining individual operators, this approach has a particular appeal at a time when no other signs of new physics have yet been discovered at the LHC.

Recent studies taking advantage of the EFT technique have considered collider signals such as monophoton [3], monojet [4–7], mono- Z/W [8, 9] and mono- b events [10], during which one (or more) particle of the SM is produced and detected in the collider, recoiling against some missing transverse energy (MET or \cancel{p}_T) associated with the DM. This work has been generalized to a set of so-called “simplified models” where the DM couples to the SM through renormalizable interactions, for example through a new mediator that can be produced on-shell [11–15].

In light of the recent Higgs discovery at the LHC [16, 17], we can expand our search in yet another avenue. In this paper we investigate the possible production of a Higgs along with DM, which is accordingly dubbed a mono-Higgs process. The observed final states are MET plus the Higgs decay products, with an invariant mass constrained to be relatively close to the true mass $m_h \approx 125$ GeV.

The focus of our article is to explore those possibilities where mono-Higgs could be the primary production mechanism for DM at the LHC. We will consider examples of both contact operators and simplified models. We begin in Section II with a discussion of LHC searches for Higgs plus MET final states, concentrating here on the $b\bar{b}$ and diphoton decay channels for the Higgs. In Section III, we present examples of higher-dimension operators coupling DM to Higgs doublets and electroweak gauge bosons. We derive constraints on the coefficients of these operators both with and without implementing a unitarity condition on the potential signal events. Motivated by the processes in the EFT description, in Section IV we introduce a simplified model with a Z' gauge boson and two Higgs doublets, where the dark matter is coupled to the heavy pseudoscalar Higgs. We demonstrate that the 14 TeV LHC can probe the parameter space of this model at low $\tan\beta$. We conclude in Sec-

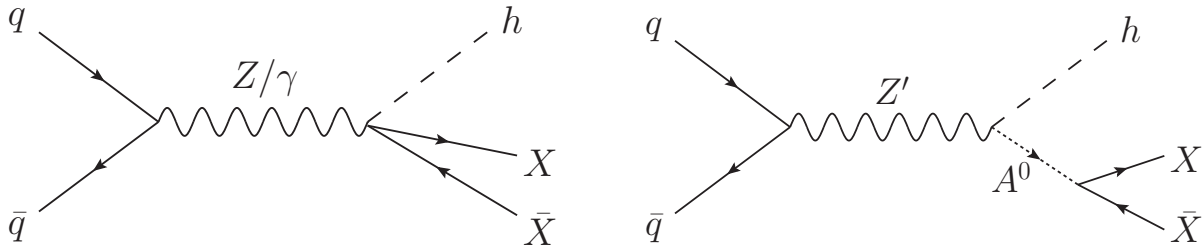


FIG. 1: Production mechanisms for dark matter plus Higgs through (left) a contact operator coupling dark matter to Zh or γh , or (right) a new Z' coupled to a two Higgs doublet model, where the new pseudoscalar A^0 decays primarily to the dark matter.

tion V.

We also note that the mono-Higgs signal has recently been discussed in Refs. [18, 19]. Ref. [18] considered contact operators coupling dark matter to SM Higgs doublets and possibly other SM states (the operators are different from the ones in this paper); however they found that for most of the operators the bounds on the cut-off scale are quite low, less than 50 GeV, which is well beyond the regime of validity for assuming a contact operator.

Ref. [19] considered a somewhat different set of operators as well as simplified models. For the “Higgs-portal”-type operators (*e.g.*, [20–22]), they find LHC limits to be much weaker than exclusion limits on Higgs invisible decay for DM masses below $m_h/2$, while direct detection is very constraining at higher masses. Ref. [19] also considered simplified models with an additional Z' , where the Higgs is produced through Higgs-strahlung of the Z' . For the case of $Z - Z'$ mass mixing, they found mono-Higgs is only able to probe large mixing angles ($\sin \theta > 0.1$), in apparent conflict with precision electroweak data. In contrast, for our scenario the Z' is produced resonantly and decays, and we have imposed the precision electroweak constraint from fits of the ρ_0 parameter.

II. Higgs + MET AT THE LHC

We consider two possible Higgs decay channels, $b\bar{b}$ and $\gamma\gamma$, as promising for observing Higgs plus MET. The $b\bar{b}$ channel has the largest branching ratio for a Higgs of mass $m_h = 125$ GeV, $\text{Br}(h \rightarrow b\bar{b}) \approx 0.577$ [23], and gives the best statistics for the signal, while the diphoton branching ratio is only $\text{Br}(h \rightarrow \gamma\gamma) \approx 2.28 \times 10^{-3}$, but is potentially a very clean channel. These channels as well as multi-lepton final states from $h \rightarrow ZZ^*$ were also studied in [19].

The dominant irreducible SM background for Higgs plus MET is Zh production with Z decaying to neutrinos. Depending on the decay channel, other SM backgrounds can also be comparable or larger. Here we rely on the ATLAS report [24] to derive bounds from LHC Run 1. For 14 TeV projections, we estimate background rates

	LHC Run 1	14 TeV
$t\bar{t}$	200	1006 ± 335
$Zb\bar{b}$	336	682 ± 26
Vh	23	142 ± 5
SM total	727 ± 11	1830 ± 336
Dim-8, fermion DM	329 ± 10	23150 ± 880
$M_{Z'} = 1$ TeV, $\tan \beta = 1$	43 ± 1	1836 ± 36

TABLE I: Background and signal events for $h \rightarrow b\bar{b}$ decay, for the cuts described in the text. The background numbers for LHC Run 1 are taken from Ref. [24] for MET > 120 GeV. For our background estimate at a 14 TeV LHC, we include only the processes listed here; uncertainties from MC statistics are shown and we include an additional 25% systematic uncertainty in deriving constraints. For the signal from a dimension-8 operator with fermion DM, Eq. (7), we take fiducial values of $\Lambda = 200$ GeV and $m_X = 1$ GeV. For the Z' case, the coupling is the upper limit allowed by the ρ_0 constraint, shown in Fig. 4.

from our own Monte Carlo event simulations and also use some results from [19].

Our dark matter models have been implemented with FeynRules 2.0 [25], and our event generation makes use of the MadGraph [26], PYTHIA [27], and Delphes [28] pipeline from parton-level to detector-level simulation.

A. Two b-jet channel

A search for $h \rightarrow b\bar{b}$ decay in association with a Z/W boson has been performed using the data of Run 1 of the LHC; the observed signal strength is compatible with that of the SM Higgs boson [24, 29]. In particular, the ATLAS collaboration presents an analysis for the $Z(\nu\bar{\nu})h$ channel in several MET bins, with the full integrated luminosity of 4.7/fb at 7 TeV and 20.3/fb at $\sqrt{s} = 8$ TeV [24]. We use these results to derive constraints on mono-Higgs for the models in this paper.

Event selection is governed by demanding two leading

b -tagged jets, with $p_T > 20$ GeV and $|\eta| < 2.5$, with the highest p_T b -tagged jet having $p_T > 45$ GeV. Multijet backgrounds are reduced by requiring $\cancel{E}_T > 120$ GeV and constraints on the azimuthal angle between the missing transverse momentum and jets: $\Delta\phi(\cancel{E}_T, b\bar{b}) > 2.8$, $\min[\Delta\phi(\cancel{E}_T, j)] > 1.5$. A lepton veto is imposed, and the $b\bar{b}$ system invariant mass must reconstruct to near the Higgs mass, $90 \text{ GeV} < m_{b\bar{b}} < 150 \text{ GeV}$. Finally, $t\bar{t}$ is suppressed by vetoing events that have any additional jets with $p_T > 30$ GeV.

Estimates of SM processes, including Zh , are compared to observed data events in three MET bins. The most important backgrounds are $Z + b\bar{b}$ and $t\bar{t}$. Making use of these published SM process estimates, we compare our signal to the data with cuts of $\cancel{E}_T > 120$ GeV, $\cancel{E}_T > 160$ GeV, and $\cancel{E}_T > 200$ GeV, and derive 95% CL upper limits on the number of possible mono-Higgs signal events.

For 14 TeV projections, we modify the 8 TeV ATLAS cuts slightly, loosening the jet veto such that up to one additional jet with $p_T > 30$ GeV is allowed, and take a cut of $\cancel{E}_T > 250$ GeV. The total integrated luminosity is 300/fb. Our estimates for background rates are shown in Table I. We find the $b\bar{b}$ channel performs better compared to the results in Ref. [19]; this appears to be due primarily to our choice of $R = 0.4$ jet clustering radius instead of $R = 0.7$, since with a larger radius the two b -jets from the Higgs decay are more often clustered together in the boosted Higgs regime.

B. Diphoton channel

The diphoton channel requires two hard photons reconstructing to the Higgs mass, large missing energy, and a veto on leptons. The dominant SM backgrounds are $Z\gamma\gamma$ and hZ/hW . Because the Higgs branching ratio to photons is so small, we find that this channel is not constraining if the 8 TeV run is considered, since there are simply not enough signal events. However, the statistics are far improved at 14 TeV. We use results for background estimates from [19], where they found that this channel can demonstrate improved sensitivity over $b\bar{b}$ (which suffers from a larger $t\bar{t}$ background). The cuts applied require $m_{\gamma\gamma} \in [110, 130]$ GeV and $\cancel{E}_T > 100, 250$ GeV at 8, 14 TeV respectively.

III. EFFECTIVE FIELD THEORY

Contact operators coupling dark matter to a Higgs doublet can potentially give rise to a mono-Higgs signal. If the dark matter is a gauge singlet, then gauge invariance implies the operator must also include other electroweak doublets. We focus on operators that give rise to a coupling of dark matter to both h and Z/γ , allowing the production of dark matter through the process

shown in Fig. 1. If the dark matter couples to two Higgs bosons, the production rate is correspondingly lower.

For the process above, we also note that a mono- Z signal is possible by reversing the roles of the h and the Z ; this rate is automatically lower by several orders of magnitude since it requires the initial production of an s -channel Higgs. For all the operators considered here, the limits from mono- Z are weaker compared to mono-Higgs.

These kinds of operators have been studied in Refs. [19, 30, 31], as well as mono-Higgs from Higgs-portal type operators in [18]. The lowest dimension SM operator that can give a Zh interaction with dark matter is

$$i(H^\dagger D_\mu H - \text{h.c.}) \rightarrow -2m_Z h Z_\mu - \langle v \rangle m_Z Z_\mu, \quad (1)$$

after electroweak symmetry breaking. This operator could be combined with singlets formed of the dark matter: $i(\phi^\dagger \partial^\mu \phi - \text{h.c.})$ for scalar DM, and $\bar{X}\gamma^\mu X$ or $\bar{X}\gamma^\mu \gamma^5 X$ for fermion DM. Because of the induced direct Z coupling to dark matter, direct detection is very constraining for $m_{\text{DM}} > 10$ GeV, while the invisible Z width is very constraining for $m_{\text{DM}} < m_Z/2$. Despite this, in the case of scalar DM Ref. [19] found that a mono-Higgs search at 14 TeV could be much more sensitive than the invisible Z width¹. We therefore do not consider this operator further.

At dimension-4 in the SM factor there is the operator

$$i[(D_\mu H)^\dagger D_\nu H - \text{h.c.}] \rightarrow m_Z(Z_\mu \partial_\nu h - Z_\nu \partial_\mu h), \quad (2)$$

concentrating on the part giving an hZ interaction. Including a DM factor, we consider

$$\frac{1}{\Lambda^3} \bar{X}\gamma^{\mu\nu} X \times i[(D_\mu H)^\dagger D_\nu H - \text{h.c.}], \quad (3)$$

neglecting the similar possibility with $\bar{X}\gamma^5\gamma^{\mu\nu} X$.

Finally there are dimension-5 SM operators [30]

$$(B_{\nu\mu} Y_H H^\dagger D^\nu H + \text{h.c.}) \quad (4)$$

$$\rightarrow \frac{\langle v \rangle}{2} (\cos \theta_w F_{\nu\mu} \partial^\nu h - \sin \theta_w Z_{\nu\mu} \partial^\nu h)$$

$$(W_{\nu\mu}^a H^\dagger t^a D^\nu H + \text{h.c.}) \quad (5)$$

$$\rightarrow -\frac{\langle v \rangle}{2} (\sin \theta_w F_{\nu\mu} \partial^\nu h + \cos \theta_w Z_{\nu\mu} \partial^\nu h)$$

where $B_{\nu\mu}$, $W_{\nu\mu}^a$ are the field strengths for $U(1)_Y$ and $SU(2)_L$, and $Z_{\nu\mu}$, $F_{\nu\mu}$ are the field strengths for Z and γ , respectively. Dimension-8 operators are formed by including a DM factor of either $\bar{X}\gamma^\mu X$ or $\bar{X}\gamma^{\mu 5} X$ for fermion DM, and either $i(\phi^\dagger \partial^\mu \phi - \text{h.c.})$ or $(\phi^\dagger \partial^\mu \phi + \text{h.c.})$ for scalar DM. Combined with the possibility of exchanging $B_{\nu\mu}$, $W_{\nu\mu}^a$ for $\tilde{B}_{\nu\mu}$, $\tilde{W}_{\nu\mu}^a$, a large number of operators

¹ The constraints on the suppression scale Λ are again of order a few hundred GeV up to a TeV for the LHC and therefore has the same problem with unitarity that we discuss below.

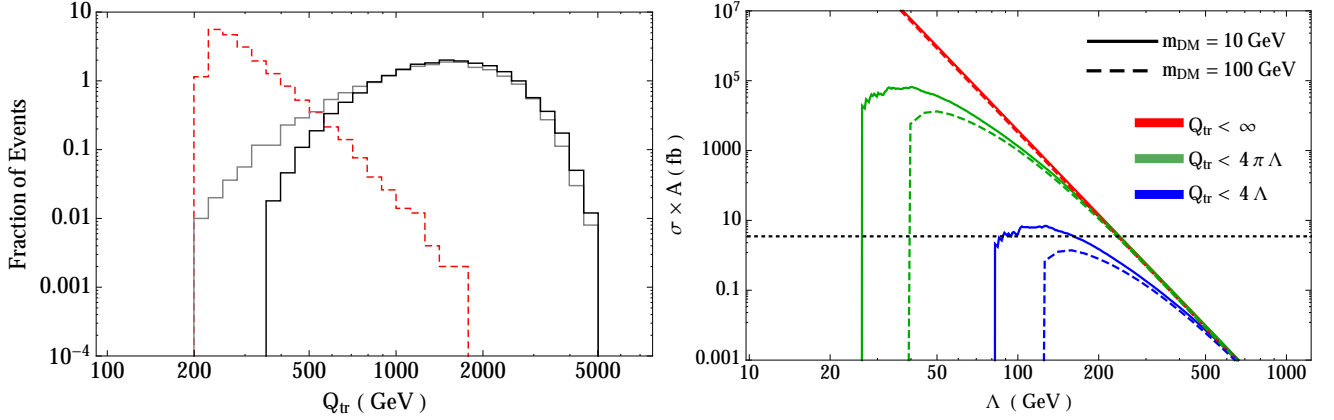


FIG. 2: (Left) Distributions (at $\sqrt{s} = 8$ TeV) for the momentum transfer Q_{tr} for 10 GeV (solid gray line) and 100 GeV (solid black line) DM, from a mono-Higgs DM signal corresponding to the operator of Eq. (7) with fermion DM. The irreducible SM background from Zh production (red dashed line) is also shown. (Right) For the same operator, the rate for mono-Higgs at 8 TeV with a cut of 120 GeV missing transverse energy. The total cross section is scaled by the fraction of events satisfying various “unitarity” conditions on Q_{tr} . The horizontal line indicates the approximate cross section that would be ruled out at 95% CL using data from Run 1 of the LHC; regions of Λ with cross sections above this line are excluded and correspond to the shaded regions in Fig. 3.

are possible. We therefore restrict our attention to two representative examples with scalar DM (ϕ) or a Dirac fermion (X):

$$\frac{1}{\Lambda^4} \frac{1}{2} (\phi^\dagger \partial^\mu \phi + \text{h.c.}) (B_{\nu\mu} H^\dagger D^\nu H + \text{h.c.}) \quad (6)$$

$$\frac{1}{\Lambda^4} \bar{X} \gamma^\mu X (W_{\nu\mu}^a H^\dagger t^a D^\nu H + \text{h.c.}) \quad , \quad (7)$$

Refs. [30, 31] discuss the complete list of possible operators, as well as further details on the relic density and gamma-ray signals of dark matter annihilation.

For the operators in Eqs. (3), and (6-7) we derive constraints on Λ as a function of DM mass from a mono-Higgs search. For LHC Run 1 data, we consider the $b\bar{b}$ channel with the weakest cut on the missing energy $\cancel{E}_T > 120$ GeV. Higher \cancel{E}_T values will necessarily require larger momentum transfer and thus lead to even larger error in the validity of the EFT, as discussed further in the following section. For 14 TeV, we obtain constraints using the diphoton channel, where we find the best results.

The LHC Run 1 lower bounds on Λ are comparable and on the order of 200 GeV for all three cases, increasing up to 300 GeV for 14 TeV projections. The related operator $\frac{1}{\Lambda^4} \bar{X} \gamma^\mu X (B_{\mu\nu} H^\dagger D^\nu H + \text{h.c.})$ was also studied in Ref. [19], where they obtained very similar bounds.

Even though one would expect the constraints on the dimension-7 operator to be stronger than for the dimension-8 ones, they are in fact slightly weaker. This is because most of the mono-Higgs signal is coming from the high momentum transfer (Q_{tr}) region, as can also be seen in Fig. 2, and the dimension-7 operator has a softer Q_{tr} dependence. This result is clearly related to the issue of validity of the EFT, as we discuss further below.

A. Unitarity

A frequent concern in this EFT approach is that, taking LHC constraints at face value, the values of Λ that can be probed correspond to energy scales accessible at the LHC. This implies a violation of perturbative unitarity at high momentum transfer, or equivalently that the EFT is no longer a valid description for LHC processes.

Fig. 2 shows the distribution for the momentum transfer Q_{tr} for the operator of Eq. (7). Compared to the naive constraint of $\Lambda \gtrsim 225$ GeV derived for the operator, it is clear that the EFT description is on shaky footing. For an s -channel mediator, the condition $Q_{tr} \lesssim 4\pi\Lambda$ is required for an expansion in the mediator mass for a perturbative theory [32] or $Q_{tr} \lesssim 2.5\Lambda$ for unitarity of the S-matrix [33]. In general the specific regime of Q_{tr} where the theory breaks down depends on the form of the operator (as well as its UV completion). Since it is not straightforward to derive UV completions for the operators here, we consider $Q_{tr} = 4\Lambda$ and $Q_{tr} = 4\pi\Lambda$ as representative of where the EFT assumption begins to suffer from large errors.

We implement three different criteria: $Q_{tr} < \infty$ (corresponding to the naive limit), $Q_{tr} < 4\pi\Lambda$, and $Q_{tr} < 4\Lambda$. More specifically, for a given Λ , we discard any events in violation and thus rescale the calculated cross section by the fraction of events satisfying this criterion at parton-level. The conditions above on the generated events should not be taken literally; they are only to indicate the size of the error in assuming a single effective operator can describe the relevant physics. This procedure gives conservative constraints, in the sense that any new physics giving rise to the operator is expected to be relevant at these scales. In general, this could lead to even

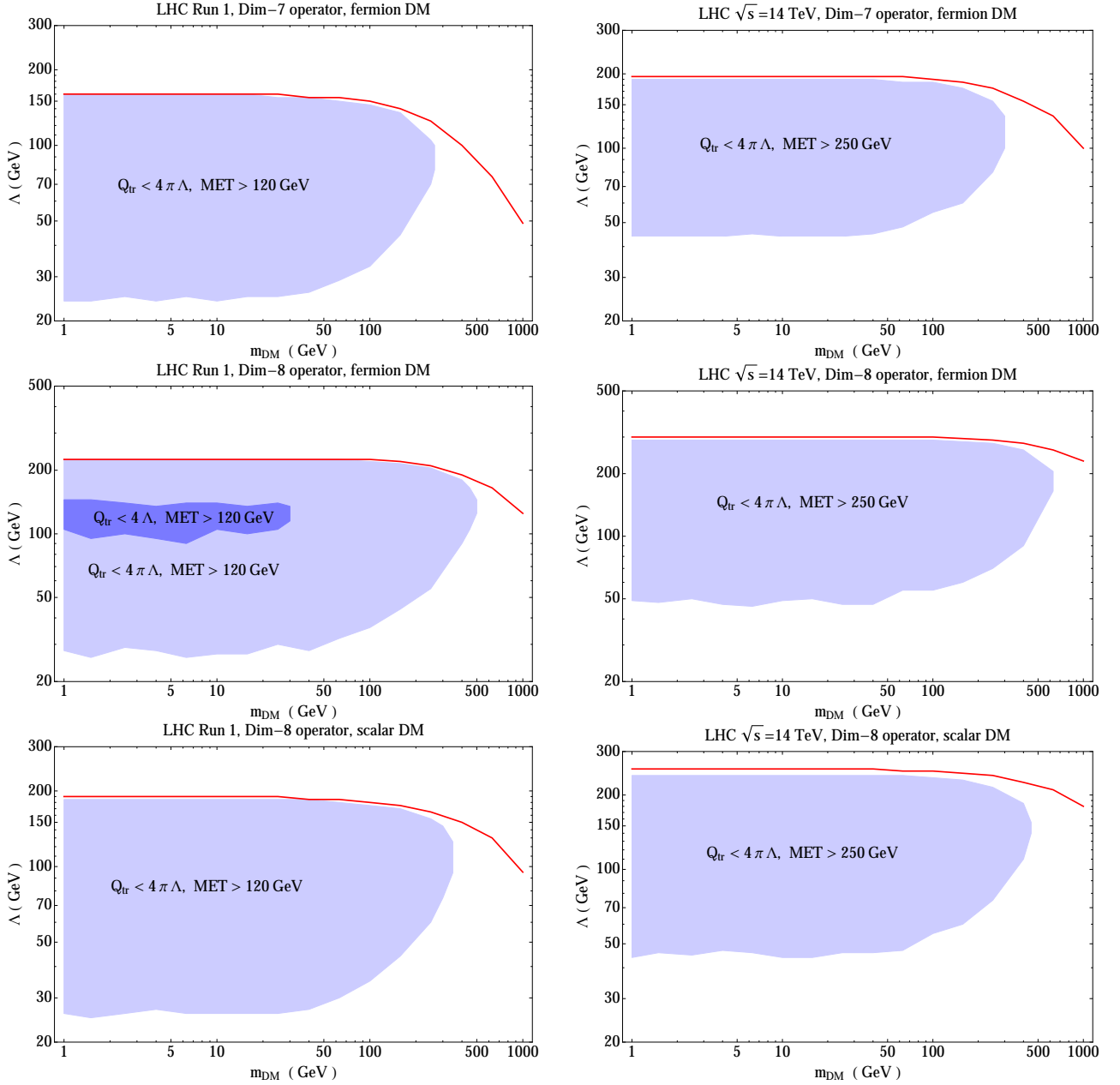


FIG. 3: 95% CL constraints from mono-Higgs on the suppression scale Λ as a function of DM mass, for operators discussed in Section III. The dimension-7 operator is $\frac{i}{\Lambda^3} \bar{X} \gamma^{\mu\nu} X [(D_\mu H)^\dagger D_\nu H - \text{h.c.}]$, the dimension-8 operator coupling to fermion DM is $\frac{1}{\Lambda^4} \bar{X} \gamma^\mu X (W_{\nu\mu}^a H^\dagger t^a D^\nu H + \text{h.c.})$, and the dimension-8 operator coupling to scalar DM is $\frac{1}{\Lambda^4} \frac{1}{2} (\phi^\dagger \partial^\mu \phi + \text{h.c.}) (B_{\nu\mu} H^\dagger D^\nu H + \text{h.c.})$. The solid lines are the lower bounds for the naive EFT result ($Q_{\text{tr}} < \infty$). The shaded regions are the excluded regions imposing the conditions on the momentum transfer $Q_{\text{tr}} < 4\pi \times \Lambda$ or $Q_{\text{tr}} < 4\Lambda$ to address the apparent violation of unitarity. The left column shows LHC Run 1 limits, derived for the $b\bar{b}$ channel with a MET cut of 120 GeV, while right column shows 14 TeV limits assuming the diphoton channel and a MET cut of 250 GeV.

stronger constraints on the model, for example from an enhanced signal in the original channel or from other new signal channels [32–34].

Our results for the operators are shown in Fig. 3, where the solid lines give the lower limit on Λ without any condition on the momentum transfer. When a condition on Q_{tr} is imposed, this weakens and shifts the bound on Λ ;

in addition, low values of Λ are no longer excluded, which we interpret as the breakdown of the EFT. This is also illustrated by Fig. 2, where we show the mono-Higgs cross section when each one of the unitarity conditions above is imposed. For very small Λ , no events satisfy the condition on Q_{tr} . As Λ is increased, more events meet the criterion until the suppression of the cross section with

large Λ takes over. The excluded region is the range of Λ where the cross section is above that observable at the LHC (indicated by the dashed line).

For the weakest condition $Q_{\text{tr}} < 4\pi\Lambda$ a constraint is possible for all operators below DM masses around a few hundred GeV. In the most restrictive case $Q_{\text{tr}} < 4\Lambda$, we find that no bound is possible for the operators in Eqs. (3,6). For the fermion DM operator in Eq. (7), a limit for a narrow range in Λ is still possible with the strongest Q_{tr} condition and 8 TeV data, but again no bound is expected at larger masses or with a 14 TeV run. Compared to the results for the 7/8 TeV runs of the LHC, the 14 TeV run does not necessarily promise a significant improvement with respect to the issue of unitarity due to the need for a stronger \cancel{E}_T cut to suppress backgrounds.

IV. DARK MATTER VIA A Z' AND HEAVY HIGGS

Motivated by the mono-Higgs processes discussed in the previous section, we construct a simple model with renormalizable interactions where the relevant states may be produced on-shell. The high-dimension operators considered previously are challenging to UV-complete; however, it is more straightforward to generalize the mono-Higgs process, as shown in Fig. 1. If the intermediate Z is instead a new Z' gauge boson, resonant production is possible; the Z' then decays to a Higgs plus an intermediate state which decays to a DM pair. Since a SM state decaying to DM is highly constrained, we consider a two-Higgs doublet extension to the standard model with $Z' \rightarrow hA^0$, where A^0 is a heavy pseudoscalar with a large branching ratio to dark matter. Below we discuss in more detail the Z' coupled to a two-Higgs doublet model (2HDM), which is sufficient to determine the mono-Higgs signal. More model-dependent details of the DM coupling to the pseudoscalar are discussed in Sec. IV C.

The gauge symmetry of the SM is extended by a $U(1)_{Z'}$, with a new massive Z' gauge boson (see, for example, [35, 36]). We assume that this sector also contains a SM singlet scalar ϕ that leads to spontaneous breaking of the symmetry and a Z' mass at a scale above electroweak symmetry-breaking. There are many choices for how the SM fermions are charged under the $U(1)_{Z'}$; for simplicity, we assume generation-independent charges for the fermions and that only the right-handed quarks u_R are charged². This allows LHC production of the Z' , but since the leptons are neutral, avoids potentially stringent constraints from searches for dilepton resonances.

For the Higgs sector we assume a Type 2 two-Higgs-doublet model, where Φ_u couples to up-type quarks and

	Φ_d	Φ_u	Q_L	d_R	u_R
$U(1)_{Z'}$	0	1/2	0	0	1/2

TABLE II: SM fermion and scalar $U(1)_{Z'}$ gauge charges. All other SM particles are neutral.

Φ_d couples to down-type quarks and leptons:

$$-\mathcal{L} \supset y_u Q \tilde{\Phi}_u \bar{u} + y_d Q \Phi_d \bar{d} + y_e L \Phi_d \bar{e} + \text{h.c.} \quad (8)$$

with hypercharge $Y = 1/2$ Higgs doublets Φ_u, Φ_d that could have Z' charges z_u, z_d . In the case we consider, only u_R and Φ_u are charged under $U(1)_{Z'}$. Our convention for the charges are shown in Table II.

After electroweak symmetry breaking, the Higgs doublets attain vevs v_u and v_d , and in unitary gauge the doublets are parametrized as

$$\begin{aligned} \Phi_d &= \frac{1}{\sqrt{2}} \begin{pmatrix} -\sin \beta H^+ \\ v_d - \sin \alpha h + \cos \alpha H - i \sin \beta A^0 \end{pmatrix} , \\ \Phi_u &= \frac{1}{\sqrt{2}} \begin{pmatrix} \cos \beta H^+ \\ v_u + \cos \alpha h + \sin \alpha H + i \cos \beta A^0 \end{pmatrix} \end{aligned} \quad (9)$$

where h, H are neutral CP-even scalars and A^0 is a neutral CP-odd scalar. Furthermore, $\tan \beta \equiv v_u/v_d$, and α is the mixing angle that diagonalizes the $h - H$ mass squared matrix.

We make some simplifying assumptions for the Higgs sector, taking h as the scalar corresponding to the observed Higgs boson with $m_h \sim 125$ GeV. The remaining scalars H, A^0, H^\pm are assumed to have masses around or above 300 GeV, in accordance with $b \rightarrow s\gamma$ constraints [37]. Fits to the observed Higgs couplings from the LHC [38] indicate that a Type 2 2HDM is tightly constrained around the alignment limit where $\sin(\beta - \alpha) \rightarrow 1$ (specifically $\beta \rightarrow \alpha + \pi/2$, $\alpha \in (-\pi/2, 0)$). In this limit, h has SM-like couplings to fermions and gauge bosons. In addition, perturbativity of the top yukawa coupling implies $\tan \beta \gtrsim 0.3$. Hence, we choose to work in the $\alpha - \beta$ parameter space where $\tan \beta \geq 0.3$ and $\alpha = \beta - \pi/2$.

The Higgs vevs lead to $Z - Z'$ mass mixing. Diagonalizing the gauge boson mass matrix, the tree-level masses of the Z and Z' bosons are given by

$$\begin{aligned} M_Z^2 &\approx (M_Z^0)^2 - \epsilon^2 [(M_{Z'}^0)^2 - (M_Z^0)^2] \\ M_{Z'}^2 &\approx (M_{Z'}^0)^2 + \epsilon^2 [(M_{Z'}^0)^2 - (M_Z^0)^2] \end{aligned} \quad , \quad (10)$$

where $(M_Z^0)^2 = g^2(v_d^2 + v_u^2)/(4\cos^2\theta_w)$ and $(M_{Z'}^0)^2 = g_z^2(z_d^2 v_d^2 + z_u^2 v_u^2 + z_\phi^2 v_\phi^2)$ are the mass-squared values in the absence of mixing. The result above is accurate to order ϵ^2 , where ϵ is a small mixing parameter given by

$$\begin{aligned} \epsilon &\equiv \frac{1}{M_{Z'}^2 - M_Z^2} \frac{gg_z}{2\cos\theta_w} (z_d v_d^2 + z_u v_u^2) \\ &= \frac{(M_Z^0)^2}{M_{Z'}^2 - M_Z^2} \frac{2g_z \cos\theta_w}{g} z_u \sin^2 \beta. \end{aligned} \quad (11)$$

² Anomaly cancellation can be achieved with a pair of colored triplet fields which are singlets with respect to $SU(2)_L$: $\psi_L(Q_z = 0, Y = -2/3)$ and $\psi_R(Q_z = -z_u, Y = -2/3)$ where z_u is the Z' charge of u_R .

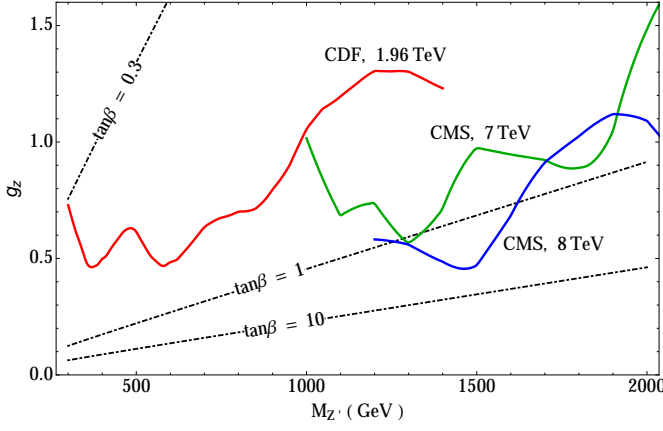


FIG. 4: 95% CL bounds on the Z' coupling g_z as a function of $M_{Z'}$. The dashed lines are upper bounds from ρ_0 parameter constraints on $Z - Z'$ mixing, given in Eq. (14), for three values of $\tan\beta = 0.3, 1, 10$. We also show upper limits from dijet resonance searches at the Tevatron and at the LHC; see text for further details.

Finally, the mass eigenstates corresponding to the observed Z boson and the hypothetical Z' boson are

$$\begin{aligned} Z^\mu &\approx W^{3\mu} \cos\theta_w - B_Y^\mu \sin\theta_w + \epsilon B_{Z'}^\mu, \\ Z'^\mu &\approx B_Y^\mu - \epsilon (W^{3\mu} \cos\theta_w - B_Y^\mu \sin\theta_w). \end{aligned} \quad (12)$$

A. Z' constraints

The $Z - Z'$ mixing leads to a modification to the Z mass, as shown in Eq. (10). This in turn affects the relation between the W and Z masses, which is expressed as a deviation of the ρ_0 parameter away from unity:

$$\rho_0 = 1 + \epsilon^2 \left(\frac{M_{Z'}^2 - M_Z^2}{M_Z^2} \right), \quad (13)$$

Current precision electroweak global fits constrain $\rho_0 = 1.0004^{+0.0003}_{-0.0004}$ [39]. Taking this result at face value, the approximate 95% upper limit

$$\rho_0 \leq 1.0009 \quad (14)$$

implies an upper limit on g_z (at fixed $\tan\beta$ and $M_{Z'}$), shown in Fig. 4. Although there are also strong LEP constraints on $Z - Z'$ mixing from, *e.g.*, precision measurements of dijets/dileptons through a Z resonance, in our case the limits are weak since the coupling to leptons is ϵ -suppressed.

There are additional g_z constraints from searches for dijet resonances from Z' decay to $q\bar{q}$, also shown in Fig. 4. We apply results from Tevatron and LHC studies, with Tevatron results [40] providing coverage for $300 \text{ GeV} \leq M_{Z'} \leq 1.4 \text{ TeV}$. We also apply 95% CL upper limits from

CMS using 7 TeV [41] and 8 TeV [42] data³, given in a model-independent form in terms of a cross section times acceptance for a narrow resonance decaying to $q\bar{q}$. An upper bound on g_z is derived by comparing our detector-level simulation to the published upper limits, assuming that the Z' width is fixed for the most part by its decay to quarks:

$$\Gamma_{Z' \rightarrow q\bar{q}} \approx \frac{g_z^2}{24\pi} z_u^2 N_c M_{Z'} \quad (15)$$

for each light-quark flavor. This is a valid approximation for the model here, assuming that there isn't a significant width for Z' decay to other new fermionic modes.

For masses below $\sim 1.3 \text{ TeV}$ (exactly the regime that we find the strongest potential mono-Higgs signal) and in particular for large $\tan\beta$, we find that the ρ_0 constraint on g_z is stronger than dijet limits. However, for $\tan\beta \lesssim 0.6$, the dijet constraints dominate even at low masses. For the remainder of the paper, for any given $M_{Z'}$ and $\tan\beta$, we will simply assume the coupling g_z is the maximum allowed by ρ_0 and dijet constraints, as given in Fig. 4.

B. Mono-Higgs signal

The mono-Higgs signal associated with DM plus Higgs production proceeds through $Z' \rightarrow hA^0$; the decay width for this to leading order in ϵ is

$$\Gamma_{Z' \rightarrow hA^0} = (g_z \cos\alpha \cos\beta)^2 \frac{|p|}{24\pi} \frac{|p|^2}{M_{Z'}^2}. \quad (16)$$

The center of mass momentum for the decay products is $|p| = \frac{1}{2M_{Z'}} \lambda^{1/2}(M_{Z'}^2, m_h^2, m_{A^0}^2)$, where λ is the Källen triangle function. Since only the Φ_u doublet couples directly to the Z' , and since the pseudoscalar component of the Φ_u scales with $\cos\beta$, this decay width is suppressed by $1/\tan^2\beta$ in the limit of large $\tan\beta$. For $\tan\beta < 1$, the rate actually increases because the allowed g_z from the precision electroweak constraint increases, at least until $\tan\beta \approx 0.6$ when dijet limits take over.

The Z' model enjoys an additional source of Higgs plus MET from the decay of $Z' \rightarrow hZ$, where the Z decays invisibly. The decay width is

$$\Gamma_{Z' \rightarrow hZ} = (g_z \cos\alpha \sin\beta)^2 \frac{|p|}{24\pi} \left(\frac{|p|^2}{M_{Z'}^2} + 3 \frac{M_Z^2}{M_{Z'}^2} \right), \quad (17)$$

which grows with smaller $M_{Z'}$ due to the $M_Z^2/M_{Z'}^2$ term. At fixed $M_{Z'}$, the mono-Higgs rate for this process is

³ The ATLAS collaboration has also presented 95% CL upper limits [43, 44], but for a narrow Gaussian in dijet mass distribution, which is not applicable to this case since there is a significant tail to the distribution at lower dijet masses.

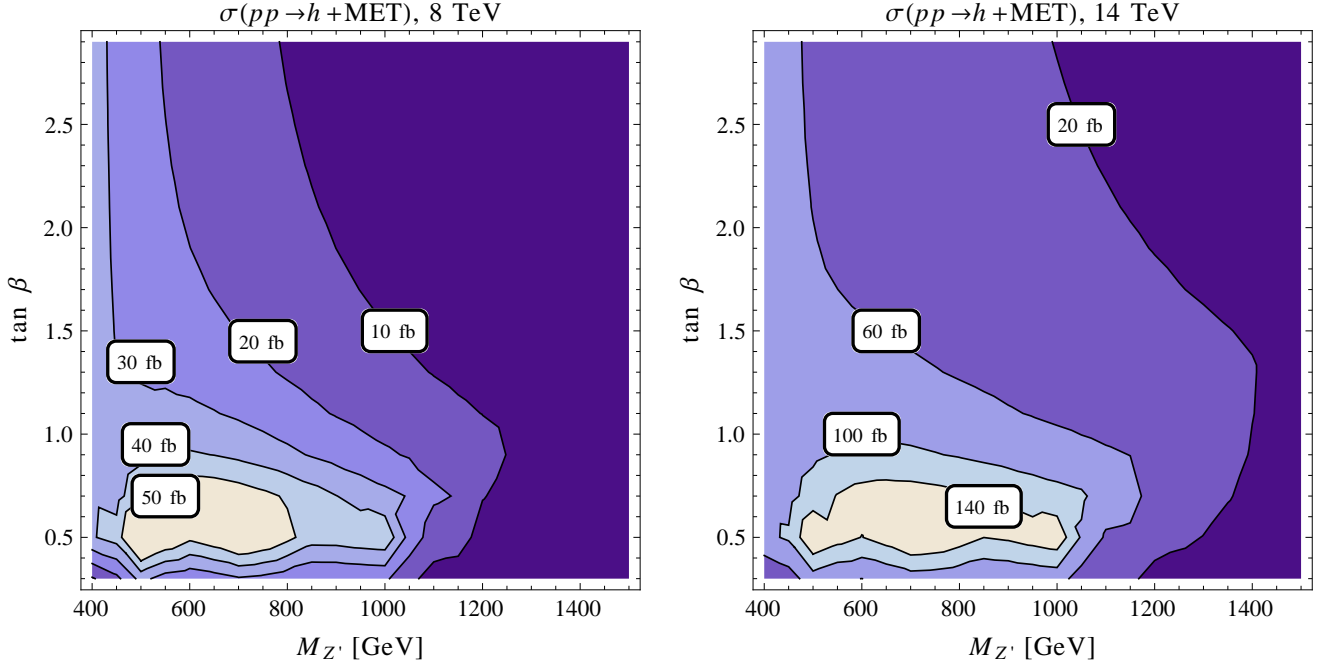


FIG. 5: Total cross sections for Higgs+MET, via a new Z' gauge boson coupled to a 2HDM, for the LHC at 8 TeV and 14 TeV. Both Higgs plus DM production from $Z' \rightarrow hA^0$ and Higgs plus MET from $Z' \rightarrow hZ, Z \rightarrow \nu\bar{\nu}$ are included. The Z' gauge coupling is fixed to be its 95% CL upper limit, as shown in Fig. 4.

almost independent of $\tan\beta$ for $\tan\beta \gtrsim 0.6$. Although the rate naïvely scales as $\sin^4\beta$, this dependence is almost exactly cancelled when we apply the upper limit on g_z from ρ_0 , which leads to an upper limit on $g_z \propto 1/(\sin^2\beta)$. This can also be seen from Eqs. (11,13). When $\tan\beta \lesssim 0.6$, the constraint on g_z is independent of $\tan\beta$ and the width is therefore suppressed by $\sin^4\beta$.

Fig. 5 shows the total mono-Higgs cross section at 8 TeV and at 14 TeV, as a function of $M_{Z'}$ and $\tan\beta$. We have fixed the coupling g_z according to its 95% CL upper bound, as discussed in the previous section. The heavy scalar masses are assumed to be 300 GeV and we take the alignment limit, $\sin(\beta - \alpha) = 1$. The branching ratio of A^0 to dark matter is taken to be 100%. Despite the larger coupling allowed at larger $M_{Z'}$, the total cross section eventually falls with $M_{Z'}$ due to pdf suppression. For large or small $\tan\beta$, the cross section also falls due to the $(\sin\beta \cos\beta)^2$ dependence in the hA^0 channel. The ratio of the two mono-Higgs rates is shown in Fig. 6. Over much of the parameter space we consider, the mono-Higgs from $Z' \rightarrow hA^0$ dominates, however $Z' \rightarrow hZ$ is a non-negligible fraction of the total signal and becomes important at low $M_{Z'}$ and also at large $\tan\beta$.

We present results for the mono-Higgs reach at the LHC in Fig. 7. For Run 1 of the LHC (combined 7 TeV and 8 TeV), we show the three 95% CL exclusion regions for the $b\bar{b}$ channel with $\cancel{E}_T > 120, 160$, and 200 GeV, where the constrained region increases with MET

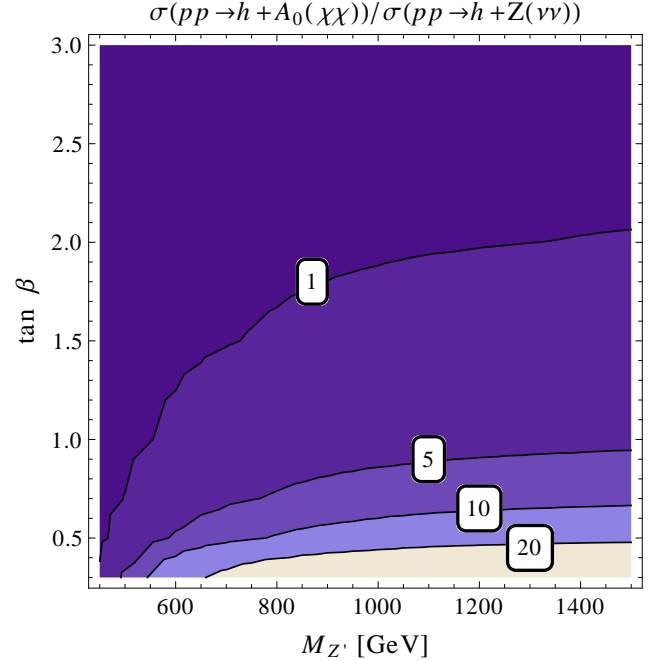


FIG. 6: Ratio of the cross sections (or, ratio of the branching ratios) for mono-Higgs from $Z' \rightarrow hA^0, A^0 \rightarrow \bar{\chi}\chi$ to mono-Higgs from $Z' \rightarrow hZ, Z \rightarrow \nu\bar{\nu}$.

cut⁴. For 14 TeV projections, we again find better overall sensitivity with a harder MET cut (taken here to be $\cancel{E}_T > 250$ GeV) to reduce SM backgrounds.

The diphoton channel is sensitive to lower cross sections compared to $b\bar{b}$ for a 14 TeV LHC, as evidenced by the reach of this channel for large values of $\tan\beta$. Although our plot cuts off at $\tan\beta = 5$, the mono-Higgs cross section is approximately constant for large $\tan\beta$ and the sensitivity can extend to much higher $\tan\beta$. However for much larger $\tan\beta$, direct searches for H, A^0 would start to be constraining [45], depending on the scalar masses. The diphoton channel also performs worse than expected at large $M_{Z'}$. This is because in our detector simulation, the energy resolution for photons deteriorates at higher energies such that the $m_{\gamma\gamma}$ peak is much broader, which limits the signal efficiency. This effect could be reduced by loosening the cut on $m_{\gamma\gamma}$, however the extent to which this would be helpful depends on the actual energy resolution in the experiment.

An appropriate question is whether other 14 TeV searches will potentially also have sensitivity for this model. For example, although data from the next LHC run will improve dijet resonance constraints, this will be mainly at large $M_{Z'}$; below 1.5 TeV it will be even more difficult to probe due to the large QCD backgrounds. Here the strongest constraint for our model was the precision electroweak fit for ρ_0 . A somewhat indirect but possibly important channel is a direct search for H, A^0 decay; for example, for H decay to SM fermions, the 14 TeV data could improve the upper limits on $\tan\beta$ significantly for the range of masses relevant here [46].

C. Dark Matter Coupling to Higgs Sector

To incorporate DM interactions, we have assumed that the CP-odd pseudoscalar A^0 of the theory possesses a large coupling to DM particles, such that the branching ratio is order one. Here we sketch out some simple models that could give rise to this kind of coupling, reserving more detailed studies for future work.

One possibility is fermion DM; for example, a pseudoscalar interaction can arise in singlet-doublet DM from a coupling to the down-type Higgs. In this model, a singlet S and electroweak doublets $D_{1,2}$ (all singlets under $U(1)_{Z'}$) are introduced, with a Lagrangian

$$-\mathcal{L} \supset \frac{1}{2} M_S^2 S^2 + M_D D_1 D_2 + y_1 S D_1 \Phi_d + y_2 S \Phi_d^\dagger D_2 + \text{h.c.}$$

The DM is the Majorana fermion that is the lightest mass eigenstate, and we require that it has a mass of at least

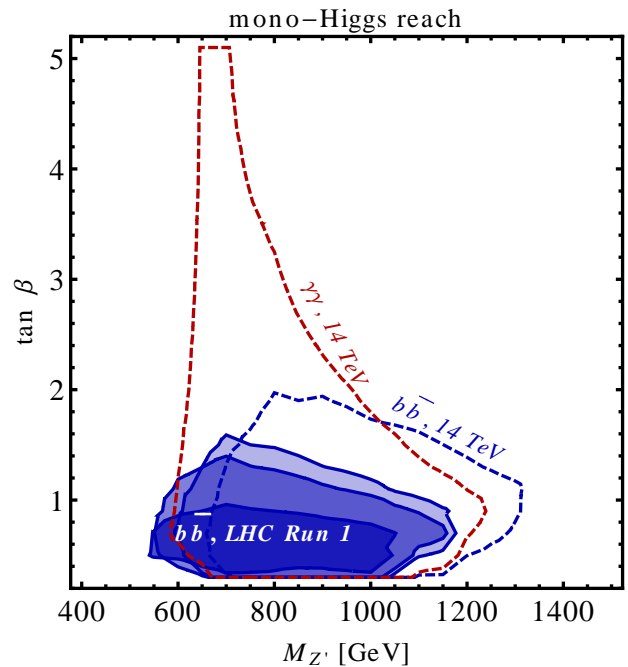


FIG. 7: 95% CL exclusion regions for the parameter space with data from Run 1 of the LHC (7 and 8 TeV, total 25/fb) for the $b\bar{b}$ channel with MET cuts of 120, 160 and 200 GeV. Dashed lines give projections for a 14 TeV LHC with 300/fb integrated luminosity for $b\bar{b}$ and diphoton channels. We only show the parameter space up to $\tan\beta = 5$ but the reach for the diphoton channel could extend to somewhat larger $\tan\beta$, since the cross section is approximately constant with $\tan\beta$.

$m_h/2$ in order to avoid bounds on the invisible width of the Higgs. In general, this state is a mixture of the singlet and the neutral components of the doublets. For more details, see for example Refs. [47, 48].

Elastic scattering off quarks can proceed via the exchange of h or H , and direct detection constraints severely restrict the parameter space for this model. However, in parts of the parameter space near the “blind spot” where the coupling through the Higgs is suppressed, the direct detection cross sections are small. This cancellation requires $\tan\theta < 0$, where $y_1 = y \cos\theta$, $y_2 = y \sin\theta$. We find it is possible to obtain large branching ratios of A^0 to DM while satisfying LUX constraints [49] for parameter values of $y = 1.5$, $\tan\theta = -2$ and masses of $M_S \approx 100 - 200$ GeV and $M_D \approx 120 - 180$ GeV.

For scalar DM, we consider a complex scalar field X , written as $X = \frac{1}{\sqrt{2}} (X_1 + iX_2)$, which is a SM singlet and has $U(1)_{Z'}$ charge $-1/4$. Then the renormalizable interactions of the DM with the Higgs sector are

$$\mathcal{L} \supset (\lambda_{dd} |\Phi_d|^2 + \lambda_{uu} |\Phi_u|^2) |X|^2 + (\lambda_{du} \Phi_d^\dagger \Phi_u X^2 + \text{h.c.}), \quad (18)$$

with all couplings taken to be real. The mass eigenstates are the real fields $X_{1,2}$ with masses $m_{1,2}^2 = m_X^2 \mp$

⁴ If we were to use the results of Ref. [19], the 8 TeV data would be unconstraining at 95% CL for almost the entire parameter space. This is partly due to the rather conservative estimates and also because the cuts are not optimal for our model.

$2\lambda_{\text{du}} \sin(2\beta)m_W^2/g^2$, where the overall mass scale m_X^2 is a free parameter. Again, the lightest component is a DM candidate.

The A^0 can decay through the term $\lambda_{\text{du}}vA^0X_1X_2$. However, this decay is not truly invisible, since the X_2 can decay to $X_1q\bar{q}$ through an off-shell A or Z' , as well as to $X_1\ell^+\ell^-$ with a somewhat smaller rate. This X_2 decay will wash out some of the missing energy; however, if the splitting between X_2 and X_1 is not too large, these additional jets or leptons are relatively soft. There is some tension for this parameter space, since larger λ_{du} is needed for an $\mathcal{O}(1)$ branching fraction, but at the same time this leads to a larger mass splitting.

Finally, DM scattering off of quarks is through h or H exchange, since Z' interactions are inelastic with a large mass splitting. It is possible to satisfy the direct detection limits from LUX if there are cancellations among the couplings λ_{dd} , λ_{uu} , and λ_{du} at the 10% level [50]. We find that couplings of order $|\lambda| \sim 0.1$ and a mass scale of $m_X \sim 100$ GeV can give rise to the desired features of the model.

V. SUMMARY AND CONCLUSIONS

The discovery of a new particle brings with it the prospect of a new signal channel for probing dark matter particle physics. In the search for dark matter, there are already many different potential avenues to its discovery, though so far without conclusive results. The simple question motivating this work is to search for possible models where dark matter production with a Higgs is the dominant discovery mode in the current generation of hadron colliders. For these models we adopted ATLAS results from the combined 7 and 8 TeV (25/fb) analysis in the $h \rightarrow b\bar{b}$ channel in order to derive constraints, and studied the sensitivity of a 14 TeV LHC in the $b\bar{b}$ as well as diphoton channels.

One way for mono-Higgs to occur is through higher dimension operators coupling dark matter to Higgs doublets and electroweak gauge bosons. LHC constraints applied to the dimension-7 or -8 operators studied here lead to the naïve conclusion that the cutoff scale Λ must be greater than 100-200 GeV. However, this is problematic from an effective field theory point of view, since such scales are low compared to the typical momentum transfer in the collider process. We have attempted to quantify the extent to which imposing a unitary constraint gives rise to a reliable (although conservative) bound on the operator. This is possible only for low dark matter masses.

We also presented a viable simplified model, where the resonant production of a Z' decaying to hA^0 and hZ allows for a potentially observable rate of mono-Higgs. This is primarily possible at low $\tan\beta$, in part because the $Z' \rightarrow hA^0$ branching fraction is $1/\tan\beta^2$ suppressed. In addition, we require the Z' gauge coupling to be near the maximum allowed from precision electroweak fits. Nevertheless, we show there is an interesting part of parameter space for low $\tan\beta$ and $M_{Z'}$ around 1 TeV, assuming the pseudoscalar A^0 decays to dark matter 100% of the time. We briefly discussed possible models that could give rise to this large pseudoscalar to invisible branching ratio. It would be interesting to pursue more detailed model-building work in this direction, taking into account direct detection or relic density considerations.

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